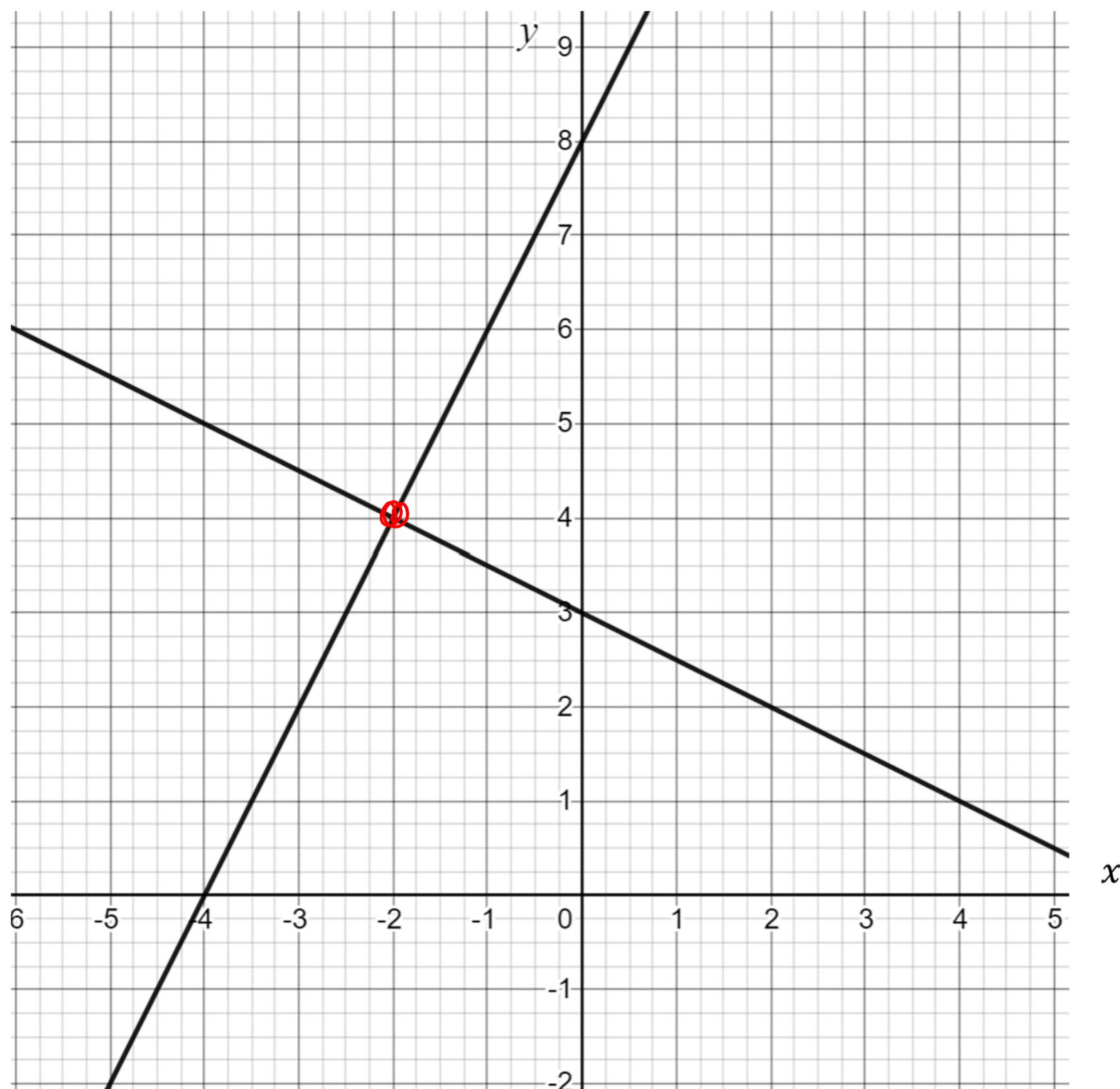


Solving Simultaneous Equations Graphically Exam Practice



Q1. The graphs of $2y + x = 6$ and $y - 2x = 8$ are drawn below:



Use the graphs to solve the following pair of equations:

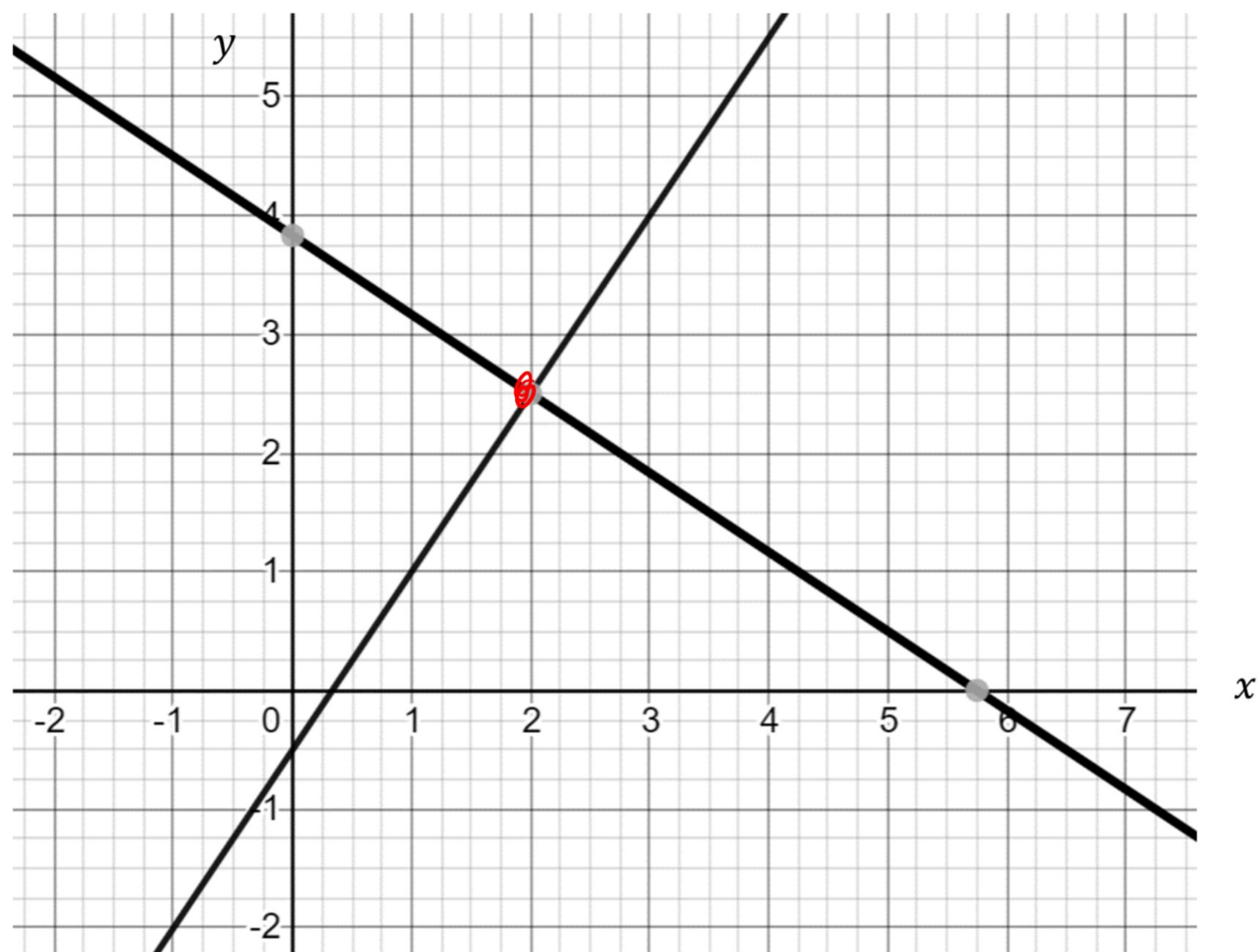
$$2y + x = 6$$

$$y - 2x = 8$$

Answer: $x = -2, y = 4$
(2 marks)



Q2. The graphs of $3x - 2y = 1$ and $4x + 6y = 23$ are drawn below:



Use the graphs to solve the following pair of equations:

$$3x - 2y = 1$$

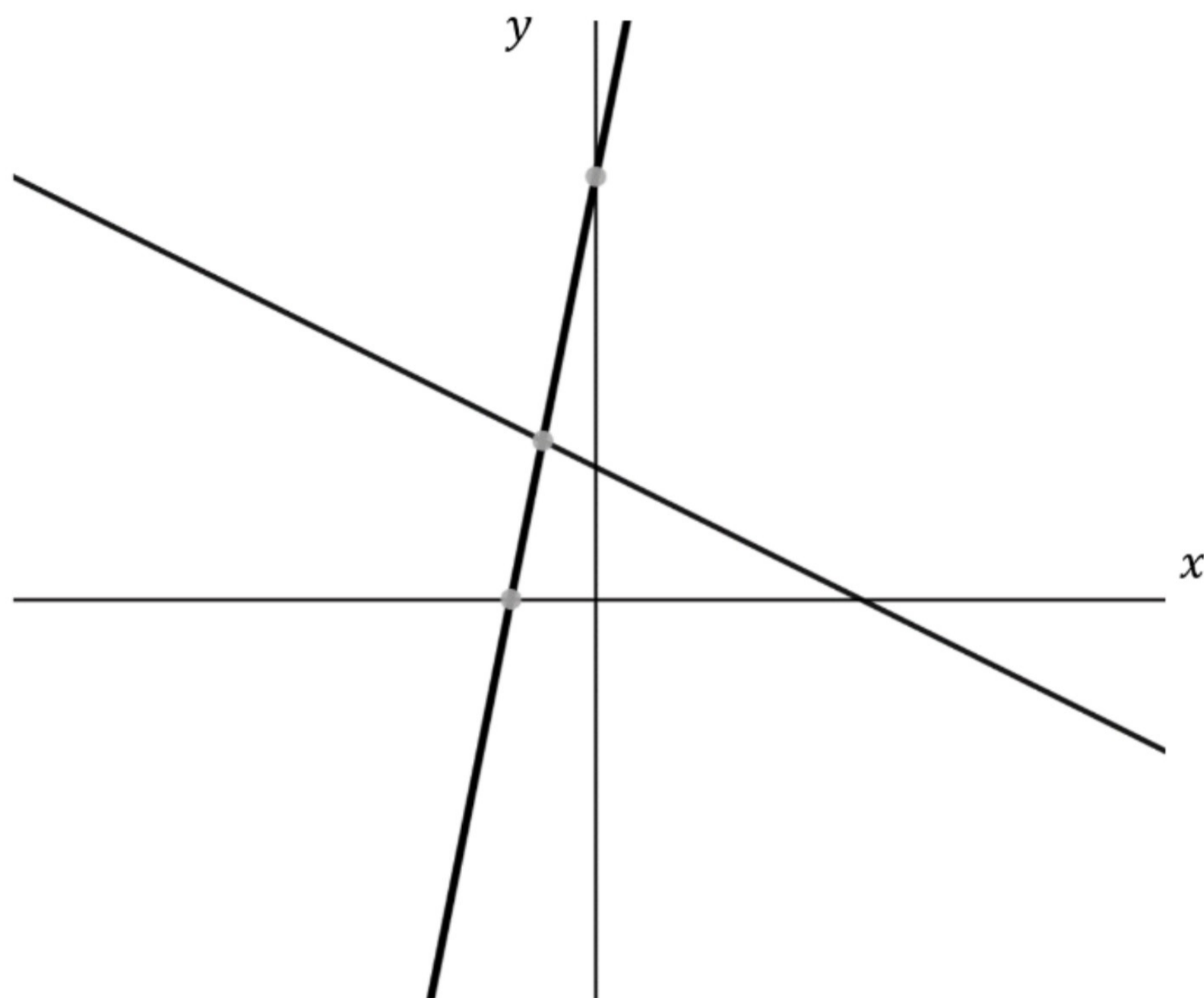
$$4x + 6y = 23$$

Answer: $x=2, y=3$

(2 marks)



Q3. A sketch of the graphs of $y - 5x = 4$ and $4x + 8y = 10$ is shown below:



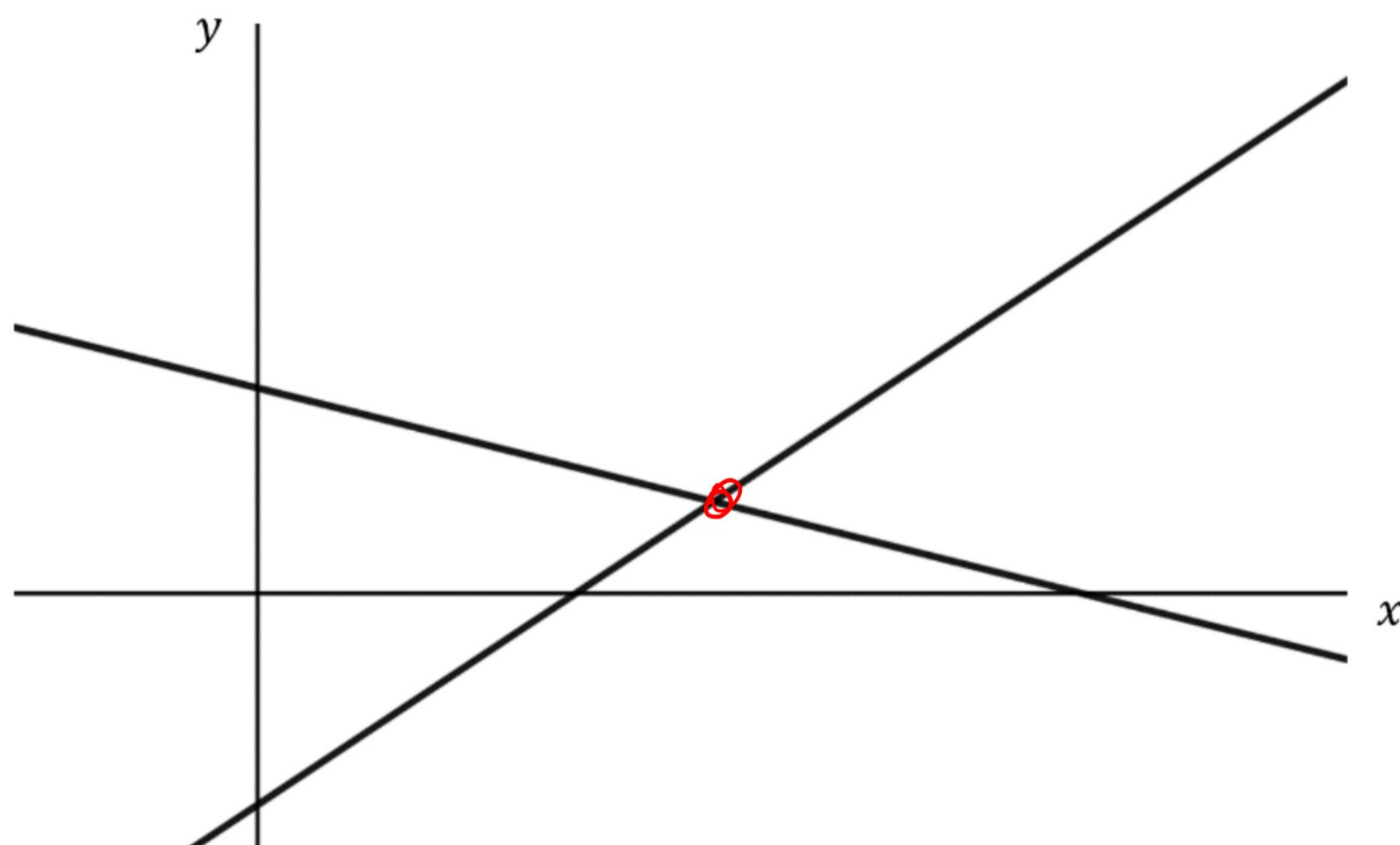
Find the exact co-ordinates of the point of intersection.

$$\begin{aligned} y - 5x &= 4 & \Rightarrow & 8y - 40x = 32 \\ \textcircled{2} \quad 8y + 4x &= 10 & - & \underline{8y + 4x = 10} \\ & & & -44x = 22 \\ & & \Rightarrow & x = -\frac{1}{2}, \text{ in } \textcircled{2} \\ 8y + 4\left(-\frac{1}{2}\right) &= 10 \\ 8y - 2 &= 10 \\ 8y &= 12 \\ y &= \frac{3}{2} \end{aligned}$$

Answer: $x = -\frac{1}{2}, y = \frac{3}{2}$
(4 marks)



Q4. A sketch of the graphs of $6x - 9y = 14$ and $2x + 8y = 12$ is shown below:



Find the exact co-ordinates of the point of intersection.

$$\begin{array}{l} \textcircled{1} \quad 6x - 9y = 14 \\ \textcircled{2} \quad 2x + 8y = 12 \end{array} \quad \left. \begin{array}{l} -6x - 9y = 14 \\ \underline{6x + 24y = 36} \end{array} \right\}$$

$$-33y = -22$$

$$y = \frac{2}{3} \text{ in (2)}$$

$$\Rightarrow 2x + 8\left(\frac{2}{3}\right) = 12$$

$$2x + \frac{16}{3} = \frac{36}{3}$$

$$2x = \frac{20}{3}$$

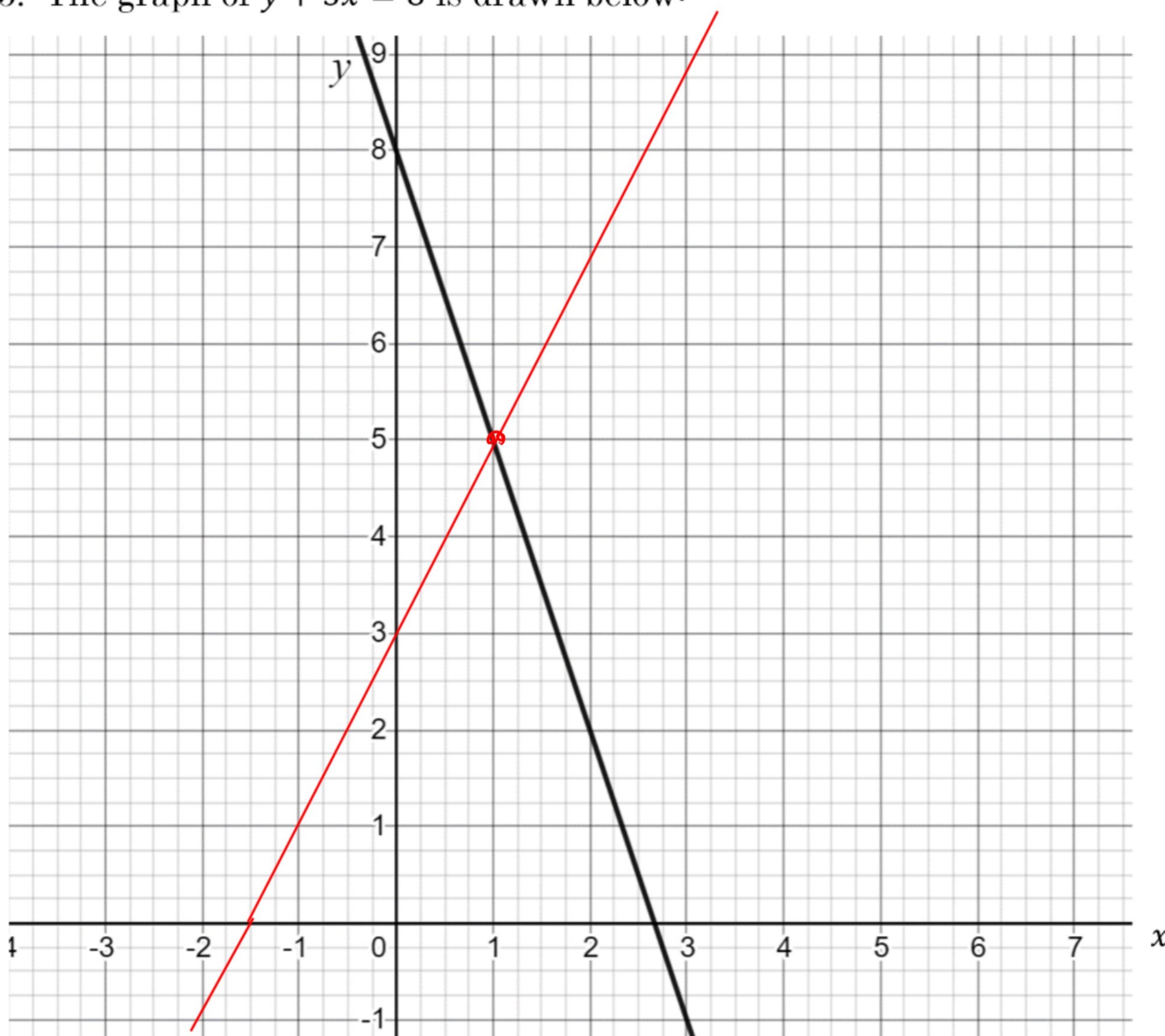
$$x = \frac{20}{6}$$

Answer: $x = \frac{20}{6}, y = \frac{2}{3}$

(4 marks)



Q5. The graph of $y + 3x = 8$ is drawn below:



By drawing a suitable line on the grid solve following pair of equations:

$y - 2x = 3$ \Rightarrow find x, y intercepts to draw line is easiest.

$y + 3x = 8$

• If $x = 0$, $y - 2(0) = 3$

$\therefore (0, 3)$ is y -intercept

• If $y = 0$, $0 - 2x = 3 \Rightarrow x = -\frac{3}{2}$

$\therefore (-\frac{3}{2}, 0)$ is x -intercept

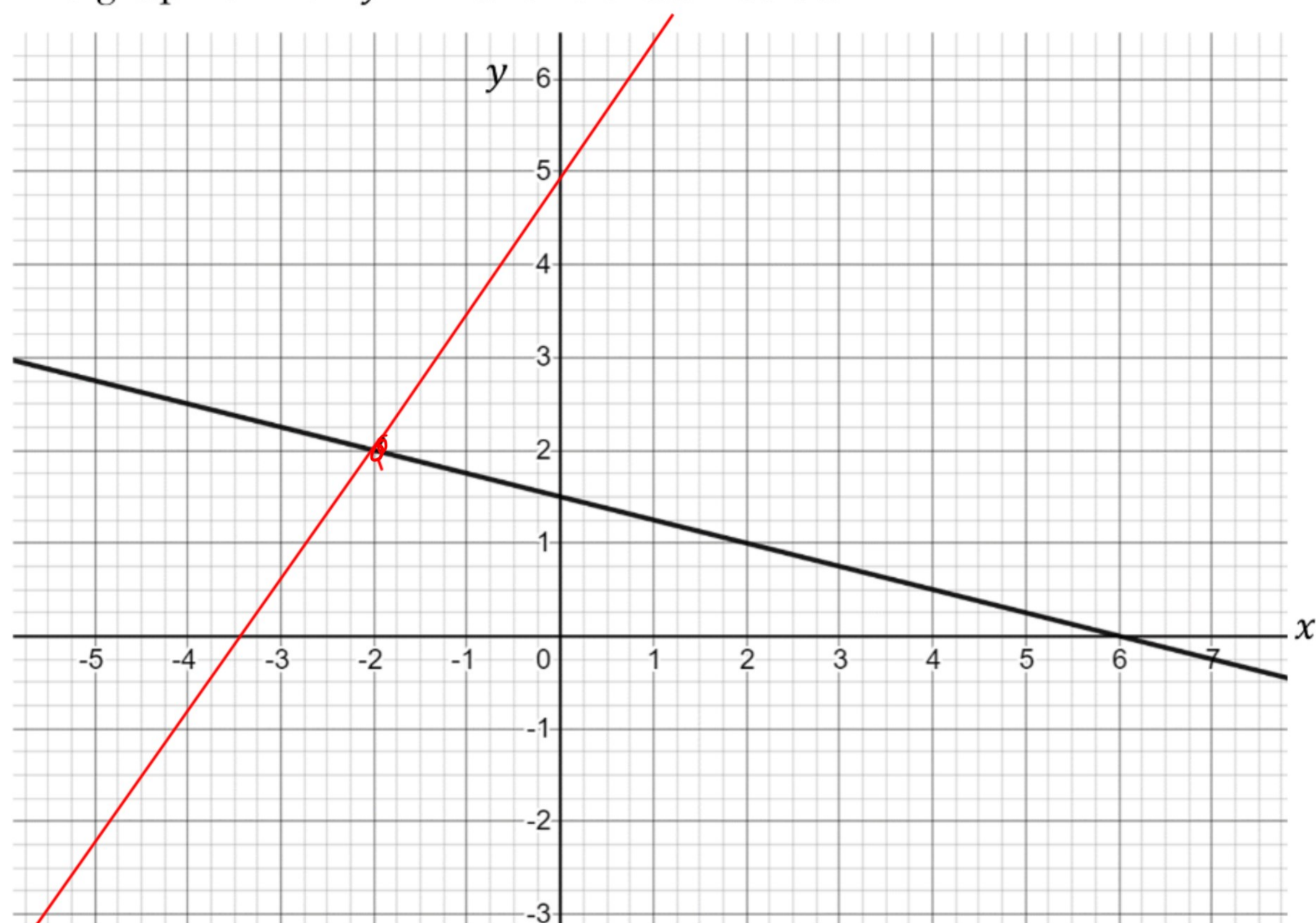
Answer: _____

$x = 1, y = 5$

(3 marks)



Q6. The graph of $x + 4y = 6$ and is drawn below:



By drawing a suitable line on the grid, solve following pair of equations:

$$2y - 3x = 10$$

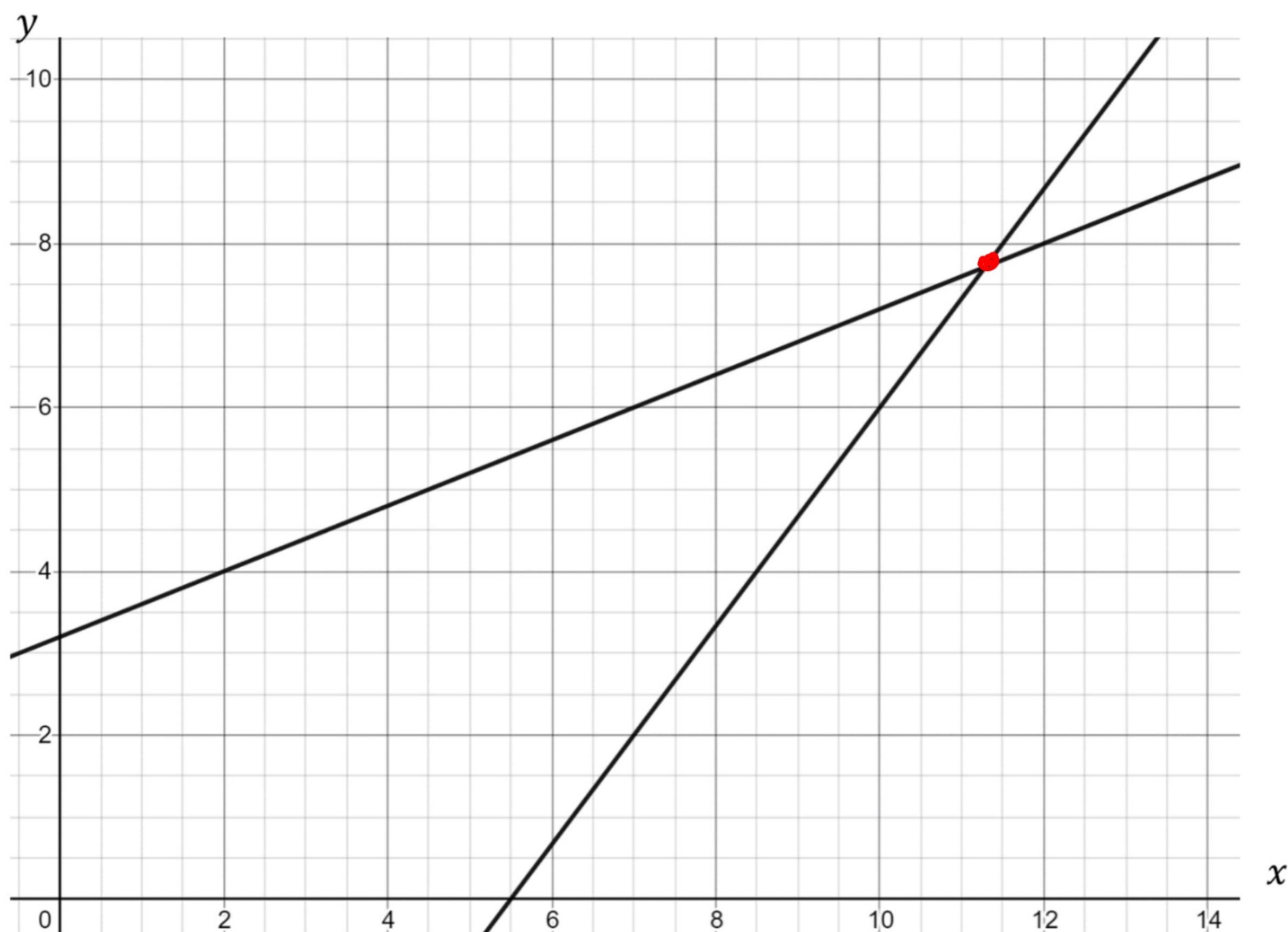
$$x + 4y = 6$$

$$\Rightarrow \begin{array}{c|c|c|} x & -1 & 0 \\ \hline y & 3.5 & 5 \end{array}$$

Answer: $x = -2, y = 2$
(3 marks)



Q7. (i) Using the grid below, estimate the solution of the equations
 $4x - 3y = 22$ and $5y - 2x = 16$



Answer: $x = 11.25, y = 7.75$
(2 marks)

(ii) How many solutions would the following set of equations have:

$$4x - 3y = 22, \quad 6y - 8x = 16$$

• gradient $6y - 8x = 16$ is $\frac{4}{3}$

$$\left(\begin{aligned} 6y &= 8x + 16 \\ y &= \frac{8x}{6} + \frac{16}{6} \end{aligned} \right)$$

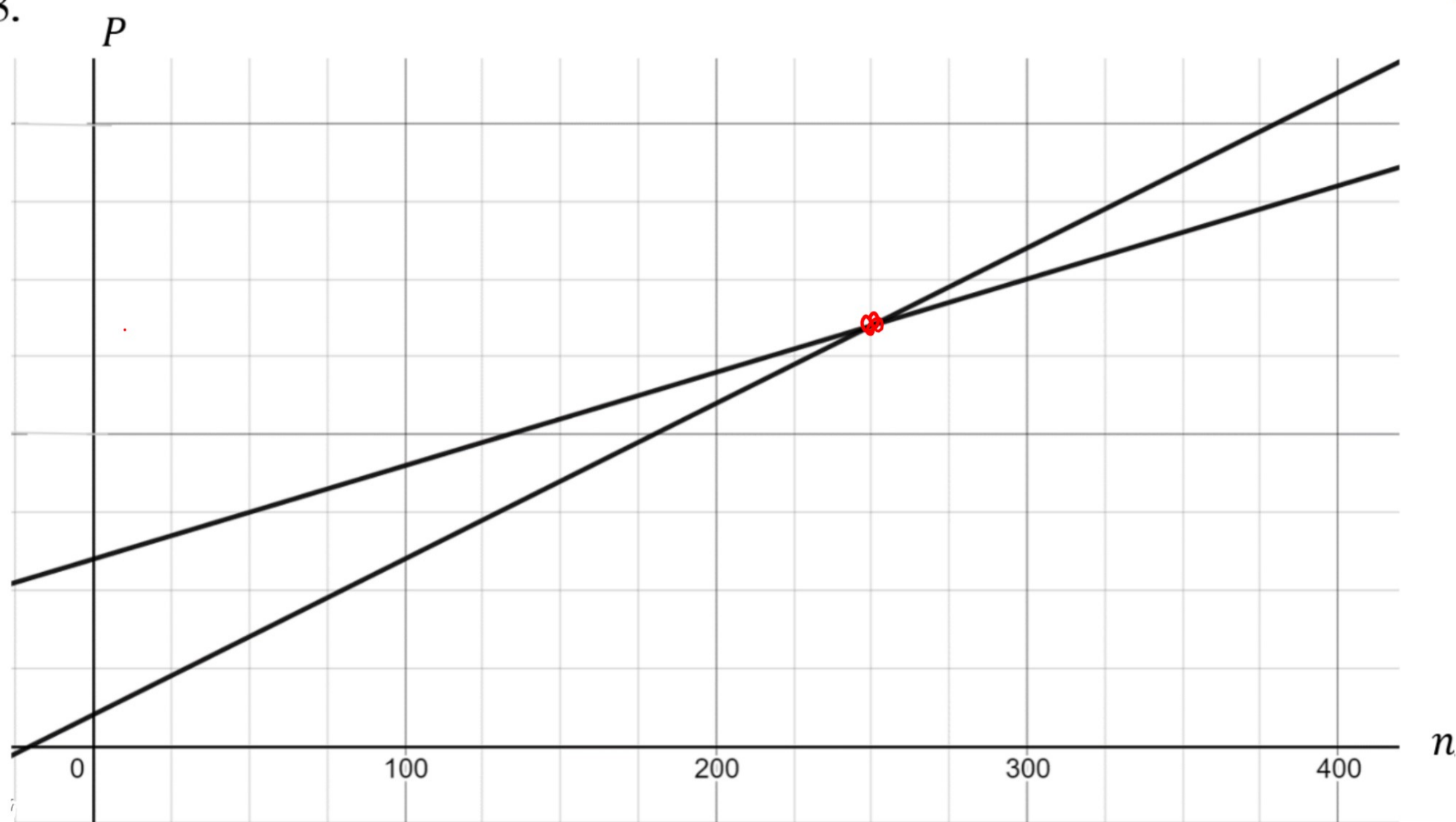
• gradient $4x - 3y = 22$ is $\frac{4}{3}$ also

• lines are parallel, so never meet.

Answer: None
(2 marks)



Q8.



In a firm, the profit P (£1000's), from the number n of items sold is modelled by 2 staff. One claims the model should be $P = 0.5n + 20$, the other says it should be $P = 0.34n + 60$.

The boss will award a staff pay-rise if the two models predict the same profit, provided that this profit exceeds £135,000. Decide if there will be a pay-rise.

- Both models agree when $n = 250$ items.
- $P = 0.5(250) + 20 \Rightarrow P = 145,000$
- $P = 0.34(250) + 60 \Rightarrow P = 145,000$
- $145,000 > 135,000$ so a payrise will be awarded.

Answer: yes, payrise
(3 marks)